

Stats: Critical Regions For A Sampling Distribution Hypothesis Test NEW

How to find critical regions for a sampling distribution hypothesis test.

We may need a calculator's Inverse Normal function.

Casio fx-991CW Classwiz	Casio fx-CG 50
1) Press HOME then select Distribution	1) Press MENU then 1 then OPTN
2) Select Inverse Normal	2) Press F5 for STAT
3) Set the Area* and the correct σ and μ	3) Press F3 for DIST and again for NORM
4) Select \blacklozenge Execute and press EXE	4) Press F3 for InvN
	5) Input Area*, SD, and mean in that order
* Area must be to the left of your point	6) Press EXE

E1: Ngoneh is conducting a sampling distribution hypothesis test using $X \sim N(40, 4)$. Find the critical region if $H_1: \mu > 40$ and the significance level is 5%.

Method If Calculator Is Allowed

Working

- | | |
|-------------------------------|-------------------|
| 1) Find the area required: | 0.95 |
| 2) Use a calculator as above: | $x > 43.3$ to 3sf |

Method If Solutions Relying On Calculator Tech Are Not Allowed

Working

- | | |
|--|---|
| 1) Find the z-value in the Percentage Points of the Normal distribution table: | 1.6449 |
| 2) Use the z-equation to find an x-value and give your critical region: | $1.6449 = \frac{x - 40}{2}$ $3.2898 = x - 40$ $x > 43.3$ to 3sf |

Questions

- A sampling distribution hypothesis test is set up for $X \sim N(80, 25)$. Find the critical region if $H_1: \mu > 80$ and the significance level is 5%.
- A sampling distribution hypothesis test is set up for $X \sim N(100, 8^2)$. Find the critical region if $H_1: \mu < 100$ and the significance level is 1%.
- A sampling distribution hypothesis test is set up for $X \sim N(64, 5)$. Find the critical region if $H_1: \mu \neq 64$ and the significance level is 5%.
- A Normally distributed variable has mean 125 and variance 36. A sample of 10 is taken to test that the mean has decreased. Find the critical region for a test at significance 1%.
- A Normally distributed variable has mean 90 and variance 40. A sample of 20 is taken to test that the mean has changed. Find the critical region for a test at significance 10%.
- A Normally distributed variable has mean 50 and standard deviation 8. A sample of 15 is taken to test that the mean has increased. Find the critical region for a test at significance 5%.

Answers

- | | | |
|----------------|-----------------------------|-----------------------------|
| 1) $x > 88.2$ | 2) $x < 81.4$ | 3) $x < 59.6 \cup x > 68.4$ |
| 4) $x < 120.6$ | 5) $x < 87.7 \cup x > 92.3$ | 6) $x > 53.4$ |